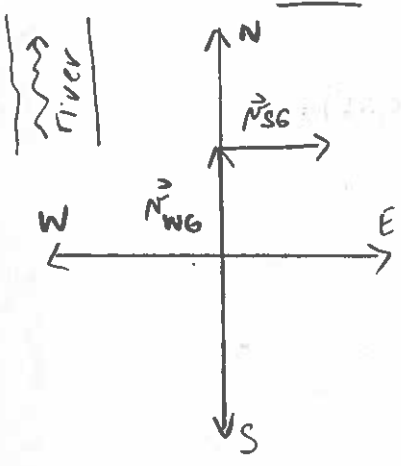


Relative Velocity - Practice

1. A swimmer has a velocity of 2.0 m/s directly across a river that is flowing at 4.0 m/s. What is the actual velocity of the swimmer? Draw vectors and clearly identify angle theta.



$$\vec{N}_{WG} = [0, 4.0] \text{ m/s}$$

$$\vec{N}_{SG} = [2.0, 0] \text{ m/s}$$

\therefore Swimmer's actual velocity is $4.5 \text{ m/s} [E63^\circ S]$

$$\vec{N}_{SW} = \vec{N}_{SG} + \vec{N}_{GW}$$

$$= [2.0, 0] + [0, -4.0]$$

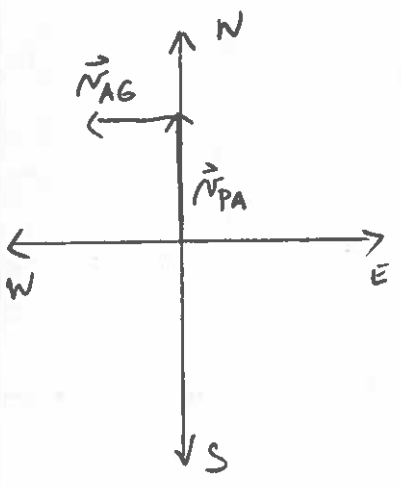
$$= [2.0, -4.0] \text{ m/s}$$

$$\|\vec{N}_{SW}\| = \sqrt{(2.0)^2 + (-4.0)^2}$$

$$= 4.5 \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{4}{2}\right) = 63^\circ$$

2. A plane is flying at 100 m/s due north with a cross wind (perpendicular to plane's velocity) of 20 m/s to the west. What is the plane's actual velocity and angel from true north?



$$\vec{N}_{PA} = [0, 100] \text{ m/s}$$

$$\vec{N}_{AG} = [-20, 0] \text{ m/s}$$

\therefore Plane's actual velocity is $1.0 \times 10^2 \text{ m/s}$
 11° W of N.

$$\vec{N}_{PG} = \vec{N}_{PA} + \vec{N}_{AG}$$

$$= [0, 100] + [-20, 0]$$

$$= [-20, 100] \text{ m/s}$$

$$\|\vec{N}_{PG}\| = \sqrt{(-20)^2 + 100^2}$$

$$= \sqrt{10400}$$

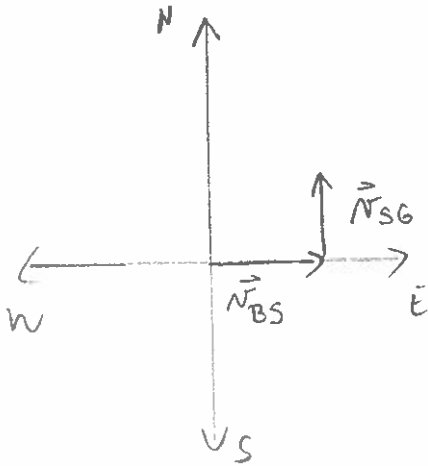
$$= 101.9804 \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{100}{20}\right)$$

$$\theta = 79^\circ [W 79^\circ N]$$

G = ground
 S = stream
 B = boat

3. A sailboat is on a heading of due East at 5.0 m/s while crossing the Gulf Stream current, which is moving 4.0 m/s due North. What is the sailboat's actual speed and heading?



$$\vec{N}_{BS} = [5.0, 0] \text{ m/s}$$

$$\vec{N}_{SG} = [0, 4.0] \text{ m/s}$$

$$\begin{aligned} \vec{N}_{BG} &= \vec{N}_{BS} + \vec{N}_{SG} \\ &= [5.0, 0] + [0, 4.0] \\ &= [5.0, 4.0] \end{aligned}$$

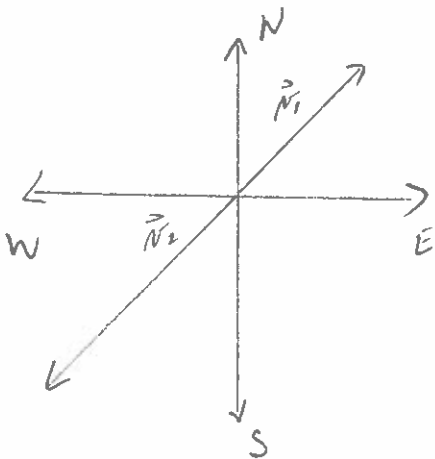
$$\begin{aligned} \|\vec{N}_{BG}\| &= \sqrt{41} \\ &= 6.4 \text{ m/s} \end{aligned}$$

$$\theta = \tan^{-1}\left(\frac{4}{5}\right)$$

$$\theta = 39^\circ$$

∴ Sailboat's actual speed is 6.4 m/s and its heading is 39° N

4. A plane leaves Atlanta flying northeast at 100 m/s. Another plane leaves Atlanta flying southwest at 150 m/s. What is their velocity relative to each other?



$$\begin{aligned} \vec{N}_{1A} &= [100 \cos 45^\circ, 100 \sin 45^\circ] \\ &= [70.7107, 70.7107] \text{ m/s} \end{aligned}$$

$$\begin{aligned} \vec{N}_{2A} &= [-150 \cos 45^\circ, -150 \sin 45^\circ] \\ &= [-106.0660, -106.0660] \text{ m/s} \end{aligned}$$

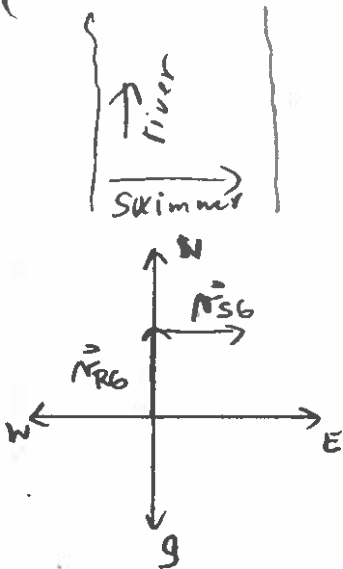
$$\begin{aligned} \vec{N}_{12} &= \vec{N}_{1A} + \vec{N}_{A2} \quad \text{And} \quad \vec{N}_{21} = \vec{N}_{2A} + \vec{N}_{A1} \\ &= [70.7107, 70.7107] + [106.0660, 106.0660] \\ &= [176.7767, 176.7767] \text{ m/s} \end{aligned}$$

$$\|\vec{N}_{12}\| = 250 \text{ m/s} \Rightarrow \|\vec{N}_{21}\| = 250 \text{ m/s}$$

$$\therefore \vec{N}_{12} = 250 \text{ m/s [NE]}$$

$$\therefore \vec{N}_{21} = 250 \text{ m/s [SW]}$$

5. A swimmer's path appears to be going directly across a river at 1.5 m/s. The current is 2.0 m/s. How fast and at what direction must she be swimming?



$$\vec{v}_{RG} = [0, 2.0] \text{ m/s}$$

$$\vec{v}_{SG} = [1.5, 0] \text{ m/s}$$

$$\theta = \tan^{-1}\left(\frac{2}{1.5}\right)$$

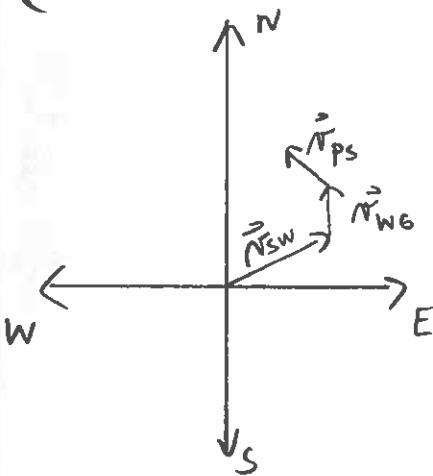
$$\theta = 53^\circ$$

$$\begin{aligned} \vec{v}_{SR} &= \vec{v}_{SG} + \vec{v}_{GR} \\ &= [1.5, 0] + [0, -2.0] \\ &= [1.5, -2.0] \text{ m/s} \end{aligned}$$

$$\begin{aligned} \|\vec{v}_{SR}\| &= \sqrt{1.5^2 + (-2.0)^2} \\ &= \sqrt{6.25} \\ &= 2.5 \text{ m/s} \end{aligned}$$

\therefore The swimmer is swimming at 2.5 m/s [E 53° S] [across 53° against the stream].

6. A ship is heading 30° N of E at 10 m/s. The ocean currents are flowing north at 1.0 m/s. A man walked across the ship 1.0 m/s in a direction perpendicular to the ship (30° W of N). Draw all the vectors. Add vectors algebraically to determine the velocity of the man relative to the earth.



$$\begin{aligned} \vec{v}_{SW} &= [10 \cdot \cos 30^\circ, 10 \cdot \sin 30^\circ] \\ &= [8.6603, 5.0] \text{ m/s} \end{aligned}$$

$$\text{Current: } \vec{v}_{WG} = [0, 1.0] \text{ m/s}$$

$$\vec{v}_{PS} = 1.0 [\text{W } 60^\circ \text{ N}]!$$

$$= [-\cos 60^\circ, \sin 60^\circ]$$

$$= [-0.5, 0.8660] \text{ m/s}$$

$$\begin{aligned} \vec{v}_{PG} &= \vec{v}_{PS} + \vec{v}_{SW} + \vec{v}_{WG} \\ &= [-0.5, 0.8660] + [8.6603, 5.0] + [0, 1.0] \\ &= [8.1603, 6.8660] \text{ m/s} \end{aligned}$$

$$\begin{aligned} \|\vec{v}_{PG}\| &= \sqrt{113.7324} \\ &= 11 \text{ m/s} \end{aligned}$$

$$\theta = \tan^{-1}\left(\frac{6.866}{8.1603}\right)$$

$$\theta = 40^\circ$$

\therefore The person's velocity relative to Earth is 11 m/s [E 40° N]

