

Notes:

PHYSICS 12

Projectile Motion In-Class Examples

1. A 2.0-kg object is thrown at an angle of 58° above horizontal. This object land on the ground 10.0 seconds later. The ground level is 40.0 m below the launching level.
 - a) Find the object's initial velocity.
 - b) Find the horizontal displacement of the object.
 - c) What is the distance between the launching point and the point the object struck the ground?
 - d) What is the final velocity of the object just before it hits the ground?

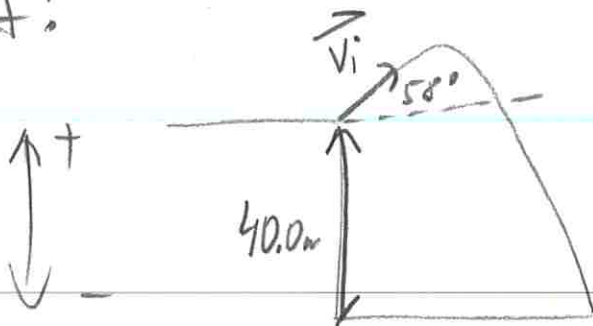
G: $m = 2.0 \text{ kg}$
 $a_y = g = 9.8 \text{ m/s}^2 [D]$
 $\theta = 58^\circ$ above horizontal
 $t_{\text{air}} = 10.0 \text{ s}$
it lands 40.0m below launching level

- Let $\vec{v}_{iy} = \|\vec{v}_i\| \cdot \sin 58^\circ = y$
- let $a_y = g = a$
- let $t_{\text{air}} = t$

R: $v_i = ? [m/s]$

$$\begin{aligned} \vec{d}_y &= -(40 + h_{\text{max}}) \\ &= -\left(40 + \frac{0 - y^2}{2a}\right) \end{aligned}$$

A:



$$= -\left(\frac{80a - y^2}{2a}\right)$$

$$t_{\text{air}} = t_{h_{\text{max}}} + t_{\text{ff}}$$

$$= \frac{-80a + y^2}{2a}$$

$$t_{\text{air}} = \frac{0 - y}{a} + \sqrt{\frac{2\vec{d}_y}{a}}$$

0/0

$$t = \frac{-y}{a} + \sqrt{\frac{2(-80a + y^2)}{2a}} \cdot \frac{1}{a}$$

$$t = \frac{-y}{a} + \sqrt{\frac{-80a + y^2}{a} \cdot \frac{1}{a}}$$

$$t = \frac{-y}{a} + \frac{1}{a} \sqrt{-80a + y^2}$$

$$t + \frac{y}{a} = \frac{1}{a} \sqrt{-80a + y^2}$$

$$a\left(t + \frac{y}{a}\right) = \sqrt{-80a + y^2}$$

$$(at + y)^2 = \left(\sqrt{-80a + y^2}\right)^2$$

$$a^2 t^2 + 2aty + y^2 = -80a + y^2$$

$$2aty = -80a - a^2 t^2$$

$$y = \frac{-v_0 a - a^2 t^2}{2at}$$

$$a = -9.8$$

$$t = 10.0$$

$$y = \frac{-80(-9.8) - (-9.8)^2(10.0)^2}{2(-9.8)(10.0)}$$

$$\underline{\underline{y = 45 \frac{m}{s} = v_{iy}}}$$

$$v_{iy} = \|v_i\| \cdot \sin \theta$$

$$\|v_i\| = \frac{v_{iy}}{\sin \theta}$$

∴ The object's initial velocity is 53.1 m/s
 58° above horizontal

$$\begin{aligned} &= \frac{45}{\sin 58^\circ} \\ &= \underline{\underline{53.1 \text{ m/s}}} \end{aligned}$$

$$b) d_x = t_{air} \cdot v_{ix}$$

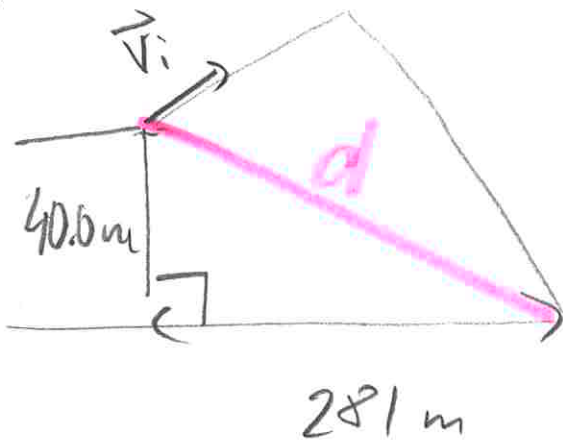
$$d_x = (10.0) (v_i \cdot \cos 58^\circ)$$

$$d_x = (10.0) (53.1) (\cos 58^\circ)$$

$$\underline{d_x = 281 \text{ m}}$$

S: The object's horizontal displacement is 281 m [R] based on the assumption that it was launched to the right.

c)



$$d^2 = 40.0^2 + 281^2$$

$$d = \sqrt{80561}$$

$$\underline{d = 284 \text{ m}}$$

S: Distance between the launching and landing point is 284 m
($= 2.8 \times 10^2 \text{ m}$).

$$d) \vec{v}_f = [v_{ix}, v_{fy}] \text{ m/s}$$

$$v_{ix} = 28.1 \text{ m/s}$$

$$v_{fy} = -\sqrt{v_{ix}^2 + 2a_y \Delta y}$$

$$= -\sqrt{0^2 + 2(-9.8)\left(-\left(40 + \frac{-45^2}{2(-9.8)}\right)\right)}$$

$$= -\sqrt{2809}$$

$$= -53 \text{ m/s}$$

$$\|\vec{v}_f\| = \sqrt{(28.1)^2 + (-53)^2}$$

$$= 59.988 \dots \text{ m/s}$$

$$= \underline{6.0 \times 10^1 \text{ m/s}}$$

∴ The object's final

velocity is $6.0 \times 10^1 \text{ m/s}$ [R62°D].

$$\theta = \tan^{-1}\left(\frac{53}{28.1}\right)$$

$$\theta = 62^\circ$$