

KEY

Name: _____
Date: _____

$$v_i = 0 \text{ m/s}$$

/20

[5] 1. A 5.0-kg object fell and spent 4.25 s in free fall. What was the height it fell from?

G: $m = 5.0 \text{ kg}$
 \uparrow $v_i = 0 \text{ m/s [D]}$
 \downarrow $t_{\text{fall}} = 4.25 \text{ s}$
 $a_y = 9.8 \text{ m/s}^2 \text{ [D]}$
 R: $d_y = ? \text{ [m]}$

A: $d_y = v_{iy}t + \frac{1}{2}a_yt^2$
 S: $= 0(4.25) + \frac{1}{2}(-9.8)(4.25)^2$
 $= -88.50625 \text{ m}$

S: The object fell from 89m.

What assumptions do you make?

● No obstacles, no other forces except \vec{F}_g ; vacuum; on Earth.

[5] 2. An object is thrown with initial velocity of 68.5 m/s 78° above horizontal. How much time does it need to reach its maximum height?

G: $\vec{v}_i = 68.5 \text{ m/s } 78^\circ \text{ above horizontal}$
 \uparrow $a_y = -9.8 \text{ m/s}^2$
 \downarrow $v_f = 0 \text{ m/s}$

S: $v_{iy} = \|\vec{v}_i\| \sin 78^\circ = 67.0031 \text{ m/s}$

R: $t_{\text{hmax}} = ? \text{ [s]}$

$t_{\text{hmax}} = \frac{0 - 67.0031}{-9.8} = \underline{\underline{6.8 \text{ s}}}$

A: $t_{\text{hmax}} = \frac{v_{fy} - v_{iy}}{a_y}$

● S: The object needs 6.8 s to reach its maximum height.

$$v_{iy} = v_i$$


$$\begin{aligned} \Delta y &= h_{\max} - 50.0 \\ &= \frac{0^2 - 45^2}{2(-9.8)} - 50.0 = 53.3163 \text{ m} \end{aligned}$$

- [5] 3. A 20-kg object was ejected straight upwards with speed of 45 m/s and landed 50.0 m above the launching level. How much time elapsed between the launching of the projectile and its landing?

G: $m = 20 \text{ kg}$
 $\vec{v}_i = 45 \text{ m/s} [\uparrow]$
 $a_y = -9.8 \text{ m/s}^2$

lands 50.0 m above launching level

R: $t_{\text{air}} = ? [s]$

A: $t_{\text{air}} = \frac{0 - v_{iy}}{a_y} + \sqrt{\frac{2\Delta y}{a_y}}$

S: $= \frac{-45}{-9.8} + \sqrt{\frac{2(-53.3163)}{-9.8}}$

$= 4.5918 + 3.2986$

$\underline{\underline{= 7.9 \text{ s}}}$

A: $t_{\text{air}} = t_{\text{hmax}} + t_{\#}$

S: 7.9 s elapsed between launching and landing.

- [5] 4. Find the initial velocity of a projectile that had initial speed of 145.0 m/s and spent 8.2 s in the air. Assume that the air resistance was negligible, there were no other forces acting on the projectile except the gravitational pull of the Earth.

- What other assumptions do you have to make in order to answer this question?

G: $v_i = 145.0 \text{ m/s}$

$t_{\text{air}} = 8.2 \text{ s}$

$a_y = 9.8 \text{ m/s}^2 [\downarrow]$

R: $\theta = ? [^\circ]$

S: $-v_{iy} = t_{\text{hmax}} \cdot a_y$

$v_{iy} = -(4.1 \times (-9.8))$
 $= 40.18 \text{ m/s}$

A: Assume $t_{\text{air}} = 2t_{\text{hmax}}$

$\Rightarrow t_{\text{hmax}} = \frac{8.2}{2} = 4.1 \text{ s}$

$\theta = \sin^{-1}\left(\frac{v_{iy}}{v_i}\right)$
 $= \sin^{-1}\left(\frac{40.18}{145.0}\right)$

$= \frac{0 - v_{iy}}{a_y}$

$\underline{\underline{= 16^\circ}}$

S: The initial velocity was 145.0 m/s 16° above horizontal.