

1. a) Consider an object A thrown vertically with velocity 40m/s [up] and an object B that is thrown 1.03 seconds after object A. At what velocity [up] must be the object B thrown in order to reach its maximum height at the same instant as the object A?

$$\text{Object A: } t_{h_{\max}} = \frac{v_{fy} - v_{iy}}{a_y} = \frac{0 - 40}{-9.8} = \underline{4.0816s}$$

$$\text{Object B: } t_{h_{\max}} = 4.0816 - 1.03 = \underline{3.0516s}$$

+ this is zero as the object stops at h_{\max}

$$v_f = v_i + at \Rightarrow \vec{v}_{iy} = \vec{v}_{iy} - at$$

$$= 0 - (-9.8)(3.0516)$$

$$= 29.91 \text{ m/s} \quad \therefore \underline{\vec{v}_{iyB} = 3.0 \times 10^1 \text{ m/s [up]}}$$

b) How does the maximum height of object A compare to the maximum height of object B?

$$\text{Object A: } h_{\max} = \frac{v_{fy}^2 - v_{iy}^2}{2a_y} = \frac{0^2 - 40^2}{2(-9.8)} = \underline{81.6 \text{ m}}$$

$$\text{Object B: } h_{\max} = \frac{0^2 - 29.91^2}{2(-9.8)} = \underline{45.6 \text{ m}}$$

$$\frac{h_{\max A}}{h_{\max B}} = \frac{81.6}{45.6} = 1.8 \quad \therefore \text{The maximum height of object A is 1.8 times greater than } h_{\max} \text{ of object B.}$$

c) How would your answer from a) change if the object B was thrown at an angle above the horizontal?

→ \vec{v}_i can be at any angle θ as long as $v_{iy} = 29.91 \text{ m/s}$
the overall answer will not change.

→ v_{ix} does not affect the answer.