

FINDING INFORMATION ABOUT MORE COMPLEX CIRCUITS

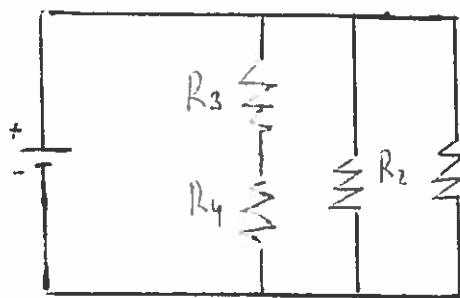
Parallel:

$$\frac{1}{\sum R} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

Series:

$$\sum R = R_1 + R_2 + \dots + R_n$$

1. Find the equivalent resistance of the electric circuit below:



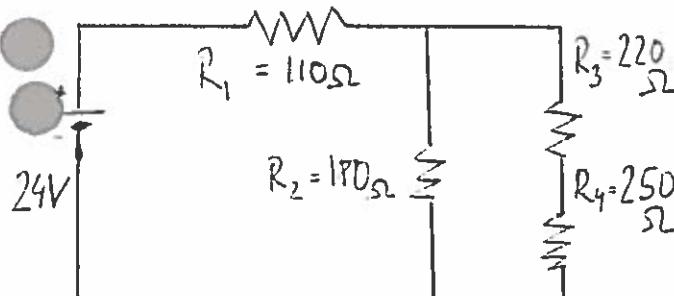
$$R_1 = 10\Omega, R_2 = 5\Omega, R_3 = 8\Omega, R_4 = 4\Omega$$

$$R_3 + R_4 = 12\Omega$$

$$\begin{aligned} \text{Step 1: } & \frac{1}{\sum R} = \frac{1}{10} + \frac{1}{5} + \frac{1}{12} = \frac{6+12+5}{60} = \frac{23}{60} \\ \therefore \sum R &= \frac{60}{23}\Omega = 2.6\Omega \end{aligned}$$

- Before using the formula for equivalent resistance for resistors in parallel R_3 and R_4 must be added using the formula for resistors in series.

2. Find the current in the electric circuit below:



$$R_3 + R_4 = 220 + 250 = 470\Omega$$

Step 1: locate all resistors in parallel R_2 , R_3 , and R_4 Step 2: add R_3 and R_4 using the formula for resistors in seriesStep 3: Find the resistance from R_2 and $(R_3 + R_4)$ using the formula for resistors in parallelStep 4: Find the equivalent resistance using the result from step 3 and adding R_1 using the formula for resistors in series

Step 5: Use Ohm's law to find the electric current

$$\begin{aligned} \text{Step 1: } & \frac{1}{\sum R_p} = \frac{1}{180} + \frac{1}{470} = \frac{470 + 180}{84600} = \frac{650}{84600} \\ \therefore \sum R_p &= \frac{84600}{650} = 130\Omega \end{aligned}$$

$$\sum R: R_1 + 130\Omega = 110 + 130 = 240\Omega$$

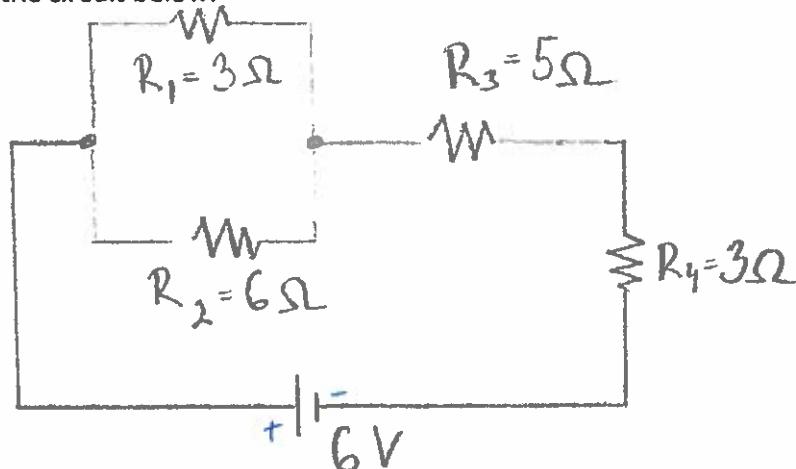
$$I = \frac{V}{R} = \frac{24}{240} = \underline{\underline{0.1A}}$$

Potential rise : from - to + 6V across the battery

Potential drop : from + to - $V_{loop} + V_3 + V_4 \Rightarrow V_{loop} = E_{rise} - E_{drop}$

3. Find as much information as you can about the electric circuit below:

- Find the equivalent resistance
- Find the electric current at the battery
- Find the electric current for each resistor
- Find the potential in every closed loop using the Second Kirchhoff's Rule
 $(\sum V_{battery} = \sum V_{resistors \text{ in a loop}})$
- Use Ohm's Law to find missing information when 2 out of 3 quantities are known



$$\begin{aligned}\sum R &= R_4 + R_3 + R_p \\ &= 3 + 5 + 2 = \underline{\underline{10\Omega}} \\ \frac{1}{R_p} &= \frac{1}{6} + \frac{1}{3} \\ &= \frac{1+2}{6} = \frac{3}{6} \\ R_p &= \frac{6}{3} = 2\Omega\end{aligned}$$

$$I_{\text{bat}} = \frac{V_{\text{bat}}}{R_{\text{eq}}} = \frac{6}{10} = \underline{\underline{0.6\text{ A}}}$$

$$I_4 = I_3 = I_{\text{battery}} = 0.6\text{ A}$$

! to find I_1 and I_2 V_1 and V_2 must be known first

$$\text{but } V_{\text{battery}} = V_4 + V_3 + V_{\text{loop}}$$

$$6 = 1.8 + 3.0 + V_{\text{loop}}$$

$$\therefore V_{\text{loop}} = 6 - 3.0 - 1.8 \\ = \underline{\underline{1.2V}}$$

$$\begin{aligned}V_4 &= (3)(0.6) = \underline{\underline{1.8V}} \\ V_3 &= (5)(0.6) = \underline{\underline{3.0V}}\end{aligned}$$

Recall: Resistors in parallel have the same voltage across each

$$V_1 = V_2 = V_{\text{loop}} = 1.2V$$

$$I_1 = \frac{V_1}{R_1} = \frac{1.2}{3} = \underline{\underline{0.4\text{ A}}} \quad I_2 = \frac{V_2}{R_2} = \frac{1.2}{6} = \underline{\underline{0.2\text{ A}}}$$