

M9

Equations and Variables

3.1 and 3.2

- So far, we have encountered three different types of algebraic statements:

equations
Always
 have an
 '=' sign

Expressions
 have no
 equal sign

Equation	Expression	Inequality
$x = 5$	$2x$	$x > 0$
$y + 7 = 11$	$x + 1$	$2x + 1 \geq 7$
$x^3 + x + 3 = 0$	$\sqrt{5}x + y$	$-5 < y$
$xy + 3 = x$	$\frac{x}{4} + 13$	$b \leq a + 2$
$\frac{1}{2}x + 6 = y$	$x^2 + y - c$	$x \neq 5$

\neq
 x is (not equal)
 To Five.
 x is different
 Than Five

An Equation Layout

$$\boxed{\text{Left Side} \quad = \quad \text{Right Side}}$$

$$LS = RS$$

$$LHS = RHS \rightarrow (\text{left hand side} = \text{right hand side})$$

- It is essential that the left side always equals the right side.
- That is why when we solve equations, we have to treat both sides the same – that is, whatever is done to the left side must be done to the right side! !

- Most equations have two types of terms: **constants (= numbers only)** and **variables (letters or letters with coefficients)**.

Examples of constants, variables, and variables with coefficients:

Constant (has no letter attached)	Variable (letters) (this means that the coefficient is either +1 or -1)	Variable with a Coefficient (numbers with letter)
5	$x = 1x$	$3 \cdot x$
-4	$xy = 1xy = 1x \cdot 1y$	$-0.5 \cdot y$
0.3	$x^2 = 1x^2$	$\frac{1}{4} \cdot x$
$\frac{1}{2}$	$-y = -1y$	$\sqrt{7}a$
10 000	-c	$5x^2$
$\frac{\sqrt{2}}{5}$	z	$-4.2z$

Name of the Operation	Addition +	Subtraction -	Multiplication •, ×, ()()	Division ÷, ÷
Name of the result	Sum	Difference	Product	Quotient