Reciprocal of a Function

- 1. Graph the original function.
- 2. Identify all x-intercepts of the original function (if they exist) and draw vertical asymptotes through each x-intercept.
- 3. Draw "helpful lines": y=1 and y=-1
- Identify all points of intersections of the original function and the line y=1 and y=-1. These points of intersection (if they exist) are the invariant points, that is, your reciprocal will pass through those points.
- 5. Determine if a horizontal asymptote exists:
 - If the numerator of the reciprocal function is a real number, HA is the x-axis.
- 6. Sketch the reciprocal following these rules:
 - Draw through invariant points
 - Avoid asymptotes
 - Plot some helpful points (especially if invariant points do not exist) using the mapping notation for the reciprocal: $(x, y) \rightarrow (x, \frac{1}{v})$
 - Reciprocal is decreasing where the original is increasing.
 - Reciprocal is increasing where the original is decreasing.