

**For each problem, you are given a table containing some values of differentiable functions  $f(x)$ ,  $g(x)$  and their derivatives. Use the table data and the rules of differentiation to solve each problem.**

| x | $f(x)$ | $f'(x)$        | $g(x)$ | $g'(x)$        |
|---|--------|----------------|--------|----------------|
| 1 | 4      | -1             | 3      | -2             |
| 2 | 3      | $-\frac{3}{2}$ | 1      | $-\frac{1}{2}$ |
| 3 | 1      | $-\frac{1}{2}$ | 2      | $\frac{3}{2}$  |
| 4 | 2      | 1              | 4      | 2              |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(2)$   
 Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(3)$

| x | $f(x)$ | $f'(x)$ | $g(x)$ | $g'(x)$ |
|---|--------|---------|--------|---------|
| 1 | 4      | -1      | 2      | 1       |
| 2 | 3      | -1      | 3      | 1       |
| 3 | 2      | -1      | 4      | 0       |
| 4 | 1      | -1      | 3      | -1      |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(2)$   
 Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(2)$

| x | $f(x)$ | $f'(x)$       | $g(x)$ | $g'(x)$ |
|---|--------|---------------|--------|---------|
| 1 | 1      | 2             | 2      | 1       |
| 2 | 3      | $\frac{3}{2}$ | 3      | 1       |
| 3 | 4      | 0             | 4      | 0       |
| 4 | 3      | -1            | 3      | -1      |

- Part 1) Given  $h_1(x) = f(x) \cdot g(x)$ , find  $h_1'(4)$   
 Part 2) Given  $h_2(x) = \frac{f(x)}{g(x)}$ , find  $h_2'(3)$

| x | $f(x)$ | $f'(x)$        | $g(x)$ | $g'(x)$ |
|---|--------|----------------|--------|---------|
| 1 | 4      | -1             | 3      | -1      |
| 2 | 3      | $-\frac{3}{2}$ | 2      | -1      |
| 3 | 1      | 0              | 1      | 0       |
| 4 | 3      | 2              | 2      | 1       |

- Part 1) Given  $h_1(x) = f(x) \cdot g(x)$ , find  $h_1'(3)$   
 Part 2) Given  $h_2(x) = \frac{f(x)}{g(x)}$ , find  $h_2'(1)$

| x | $f(x)$ | $f'(x)$        | $g(x)$ | $g'(x)$       |
|---|--------|----------------|--------|---------------|
| 1 | 4      | -1             | 3      | -2            |
| 2 | 3      | $-\frac{3}{2}$ | 1      | 0             |
| 3 | 1      | 0              | 3      | $\frac{3}{2}$ |
| 4 | 3      | 2              | 4      | 1             |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(3)$   
 Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(2)$   
 Part 3) Given  $h_3(x) = f(x) \cdot g(x)$ , find  $h_3'(4)$   
 Part 4) Given  $h_4(x) = \frac{f(x)}{g(x)}$ , find  $h_4'(2)$   
 Part 5) Given  $h_5(x) = (f(x))^2$ , find  $h_5'(2)$   
 Part 6) Given  $h_6(x) = f(g(x))$ , find  $h_6'(3)$

6)

| $x$ | $f(x)$ | $f'(x)$        | $g(x)$ | $g'(x)$       |
|-----|--------|----------------|--------|---------------|
| 1   | 2      | 2              | 3      | -2            |
| 2   | 4      | $\frac{1}{2}$  | 1      | 0             |
| 3   | 3      | $-\frac{3}{2}$ | 3      | $\frac{3}{2}$ |
| 4   | 1      | -2             | 4      | 1             |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(3)$
- Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(3)$
- Part 3) Given  $h_3(x) = f(x) \cdot g(x)$ , find  $h_3'(3)$
- Part 4) Given  $h_4(x) = \frac{f(x)}{g(x)}$ , find  $h_4'(1)$
- Part 5) Given  $h_5(x) = (f(x))^2$ , find  $h_5'(1)$
- Part 6) Given  $h_6(x) = f(g(x))$ , find  $h_6'(3)$

7)

| $x$ | $f(x)$ | $f'(x)$       | $g(x)$ | $g'(x)$       |
|-----|--------|---------------|--------|---------------|
| 1   | 3      | -1            | 1      | 2             |
| 2   | 2      | -1            | 3      | $\frac{3}{2}$ |
| 3   | 1      | $\frac{1}{2}$ | 4      | 0             |
| 4   | 3      | 2             | 3      | -1            |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(1)$
- Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(1)$
- Part 3) Given  $h_3(x) = f(x) \cdot g(x)$ , find  $h_3'(4)$
- Part 4) Given  $h_4(x) = \frac{f(x)}{g(x)}$ , find  $h_4'(3)$
- Part 5) Given  $h_5(x) = (f(x))^2$ , find  $h_5'(2)$
- Part 6) Given  $h_6(x) = f(g(x))$ , find  $h_6'(4)$

8)

| $x$ | $f(x)$ | $f'(x)$        | $g(x)$ | $g'(x)$ |
|-----|--------|----------------|--------|---------|
| 1   | 2      | 2              | 1      | 1       |
| 2   | 4      | 0              | 2      | 1       |
| 3   | 2      | $-\frac{3}{2}$ | 3      | 1       |
| 4   | 1      | -1             | 4      | 1       |

- Part 1) Given  $h_1(x) = f(x) + g(x)$ , find  $h_1'(4)$
- Part 2) Given  $h_2(x) = f(x) - g(x)$ , find  $h_2'(1)$
- Part 3) Given  $h_3(x) = f(x) \cdot g(x)$ , find  $h_3'(2)$
- Part 4) Given  $h_4(x) = \frac{f(x)}{g(x)}$ , find  $h_4'(1)$
- Part 5) Given  $h_5(x) = (f(x))^2$ , find  $h_5'(1)$
- Part 6) Given  $h_6(x) = f(g(x))$ , find  $h_6'(2)$

## Answers to (ID: 1)

$$1) h_1'(2) = -2$$

$$h_2'(3) = -2$$

$$2) h_1'(2) = 0$$

$$h_2'(2) = -2$$

$$3) h_1'(4) = -6$$

$$h_2'(3) = 0$$

$$4) h_1'(3) = 0$$

$$h_2'(1) = \frac{1}{9}$$

$$5) h_1'(3) = \frac{3}{2}$$

$$h_2'(2) = -\frac{3}{2}$$

$$h_3'(4) = 11$$

$$h_4'(2) = -\frac{3}{2}$$

$$h_5'(2) = -9$$

$$h_6'(3) = 0$$

$$6) h_1'(3) = 0$$

$$h_2'(3) = -3$$

$$h_3'(3) = 0$$

$$h_4'(1) = \frac{10}{9}$$

$$h_5'(1) = 8$$

$$h_6'(3) = -\frac{9}{4}$$

$$7) h_1'(1) = 1$$

$$h_2'(1) = -3$$

$$h_3'(4) = 3$$

$$h_4'(3) = \frac{1}{8}$$

$$h_5'(2) = -4$$

$$h_6'(4) = -\frac{1}{2}$$

$$8) h_1'(4) = 0$$

$$h_2'(1) = 1$$

$$h_3'(2) = 4$$

$$h_4'(1) = 0$$

$$h_5'(1) = 8$$

$$h_6'(2) = 0$$