

### CONTINUOUS EXTENSION OF $f(x)$ TO $x=c$

- A function may have a limit even at a point where it is not defined. If  $f(c)$  is not defined, but  $\lim_{x \rightarrow c} f(x) = L$  exists, we can define a new function  $F(x)$  by the rule:

$$F(x) = \begin{cases} f(x), & \text{if } x \text{ is in the domain of } f(x) \\ L, & \text{if } x = c \end{cases}$$

- $F(x)$  is called the continuous extension of  $f$  to  $x=c$ .

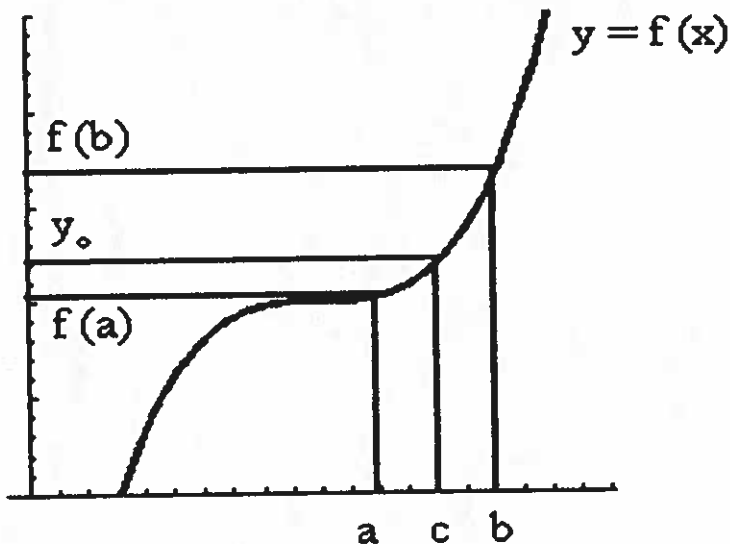
### COMPOSITES

#### THEOREM:

- If  $f$  is continuous at  $c$  and  $g$  is continuous at  $f(c)$ , then the composite  $g(f(c))$  is continuous at  $c$ .

### THE INTERMEDIATE VALUE THEOREM for continuous functions.

- A function  $y=f(x)$  that is continuous on a closed interval  $(a, b)$  takes on every value between  $f(a)$  and  $f(b)$ . In other words, if  $y_0$  is any value between  $f(a)$  and  $f(b)$ , then  $y_0=f(c)$  for some  $c$  in  $(a, b)$ .



Describe REMOVABLE DISCONTINUITY:

Give a couple of examples of removable discontinuity:

Textbook p84-86 #1-16, # 19, 21, 23, 27,29, #33-36 (#41-50 as many as you can) and #54-59